

# Thermal diffusivity measurement of Zn, Ba, V, Y and Sn doped Bi-Pb-Sr-Ca-Cu-O ceramics superconductors by photoacoustic technique

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The simple open photoacoustic cell technique is demonstrated for measuring the thermal diffusivity of the Zn, Ba, V, Y and Sn doped Bi-Pb-Sr-Ca-Cu-O superconducting ceramic samples. It is based upon the measurement of the photoacoustic signal as a function of the modulation frequency in the region where the sample thickness,  $l_s$ , equal to the thermal diffusion length of the sample,  $\mu_s$ . The obtained thermal diffusivity values of Ba, V, Y and Sn doped in Bi-Pb-Sr-Ca-Cu-O system increase with the increasing dopant concentration at Ca side. However, the thermal diffusivity values of Zn doped sample decrease with the increasing of dopant concentration in the system. The measured thermal diffusivity value was found to be very dependent on the dopant atom and dopant concentration.

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## 1. Introduction

After the discovery the formation of the high  $T_c$  phase (2223) in Bi-Pb-Sr-Ca-Cu-O system, intensive experimental work has been done by many researchers to enhance the  $T_c$  value by addition of dopant in the system [1–3]. However, there seems to exist no systematic investigation of the thermal properties of the system in the literature. In this paper, we describe the use of the open photoacoustic cell (OPC) technique to obtain the thermal diffusivity of  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{M}_x\text{Cu}_3\text{O}_\delta$ , (where  $M = \text{Zn, Ba, V, Y}$  and  $\text{Sn}$  and  $x = 0.02\text{--}0.10$ ) superconducting ceramic.

The theory of the photoacoustic effect in solid was first described by Rosencwaig and Gersho [4]. Applying the simple one dimensional thermal diffusion model of RG, the pressure fluctuation,  $P_{\text{th}}$  in the air chamber of the open photoacoustic cell detection given by [5–8]

$$P_{\text{th}} = \frac{\gamma P_0 I_0 (\alpha_g \alpha_s)^{1/2}}{2\pi l_g T_0 k_s f} \frac{e^{j(\omega t - \pi/2)}}{\sin h(l_s \sigma_s)} \quad (1)$$

where  $\gamma$  is the air specific heat ratio,  $P_0(T_0)$  are the ambient pressure (temperature),  $I_0$  is the absorbed light intensity,  $f$  is the modulation frequency,  $l_i$ ,  $k_i$  and  $\alpha_i$  are the length, thermal conductivity and thermal diffusivity of material  $i$ , respectively. The subscript  $i$  denotes the sample (s) and gas (g) media. Besides that,  $\sigma_i = (1 + j)\alpha_i$  and  $\alpha_i = (\pi f / \alpha_i)^{1/2}$ , is the complex thermal diffusion coefficient of material  $i$ . According to this model, the heat generated in the sample will dif-

fuse from the sample to the gas in immediate contact with the sample. In this process, an important parameter involved is the diffusion length of the sample  $\mu_s$ , which can be defined in terms of the thermal diffusivity by [9]

$$\mu_s = \sqrt{\alpha / (\pi f)} \quad (2)$$

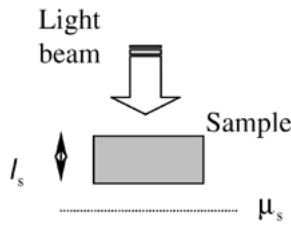
It meant that,  $\mu_s$  decreases with the increasing modulation frequency. At very low frequency ( $f < f_c$ ) or  $\mu_s > l_s$  for the thermally thin sample, the amplitude of the photoacoustic (PA) signal decreases as  $f^{-1.5}$  one increases the modulation frequency. In contrast, at high modulation frequencies ( $f > f_c$ ) or  $\mu_s < l_s$  for a thermally thick sample, the amplitude of PA signal decreases exponentially with the modulation frequency as  $(1/f) \exp(-a\sqrt{f})$ , where  $a$ , is a parameter defined as  $a = l_s \sqrt{\pi / \alpha_s}$ . For a characteristic frequency, say  $f = f_c$  when the diffusion length becomes equal to sample thickness. The thermal diffusivity can then be calculated by applying the Equation 2 which correspond to the situation  $l_s = \mu_s$ , one has [10, 11]

$$\alpha_s = \pi f_c l_s^2 \quad (3)$$

The three phenomena considered in this technique is schematically displayed in Fig. 1. However, for a plate shaped solid samples surrounded by the air, the thermoelastic bending of the sample cannot be neglected. This effect is essentially due to the temperature gradient

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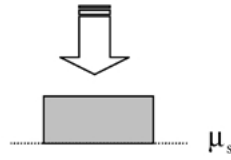
### Thermally thin sample



$$\mu_s > l_s \text{ when } f < f_c$$

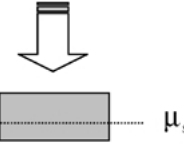
$$S \sim f^{-1.5}$$

### Thermally thick sample



$$\mu_s = l_s \text{ when } f = f_c$$

$$\alpha = \pi f_c l_s^2$$



$$\mu_s < l_s \text{ when } f > f_c$$

$$S \sim (1/f) \exp(-a\sqrt{f})$$

Figure 1 Summary of three phenomena considered in present Open Photoacoustic Cell (OPC) technique.

inside the sample along the thickness axis. This temperature gradient caused displacement along the radial direction of the sample and induces a bending along the sample thickness axis (drum effect). This has been demonstrated by Perondi and Miranda [12] where the PA signal becomes  $f^{-1}$  dependence for a thermally thick sample.

## 2. Experimental procedure

The superconducting ceramic samples of  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Zn}_x\text{Cu}_3\text{O}_8$  ( $x = 0.02-0.10$ ),  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Ba}_x\text{Cu}_3\text{O}_8$  ( $x = 0.02-0.10$ ),  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{V}_x\text{Cu}_3\text{O}_8$  ( $x = 0.05-0.10$ ),  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Y}_x\text{Cu}_3\text{O}_8$  ( $x = 0.02-0.10$ ) and  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Sn}_x\text{Cu}_3\text{O}_8$  ( $x = 0.05-0.10$ ) were prepared from a mixtures of high purity (99.9%)  $\text{Bi}_2\text{O}_3$ ,  $\text{PbO}$ ,  $\text{SrCO}_3$ ,  $\text{CaCO}_3$ ,  $\text{M}'$  ( $\text{M}' \equiv \text{ZnO}_2$ ,  $\text{BaCO}_3$ ,  $\text{V}_2\text{O}_5$ ,  $\text{Y}_2\text{O}_3$  or  $\text{SnO}_2$ ) and  $\text{CuO}$  powders. Firstly, the powders were ball-milled for 24 hours. Then, the mixture was first calcined at  $800^\circ\text{C}$  for 24 hours and the second calcination was done at  $830^\circ\text{C}$  for 14 hours with intermediate grindings in order to ensure the homogeneity. The mixture was pressed into pellets and sintered at  $855^\circ\text{C}$  for 150 hours. The resulting materials were all crystal-like black pellets. After polishing, the thickness of these samples was between 0.44 mm and 0.90 mm as summaries in Table I.

The experimental set up of the OPC configuration is shown in Fig. 2. It consists of mounting the pallet-shaped sample directly onto an electret microphone (Cirkit product, UK) with a circular hole of 2.5 mm diameter by employing silicon grease. Thus, the sample and the microphone diaphragm will form a small photoacoustic cell with the air volume is  $7.85 \text{ mm}^3$ . The argon-ion laser (Omnichrome 543) beam, which after being mechanically chopped by an optical chopper (Stanford Research System SR540) was focused onto the sample. As a result of the periodic heating of the sample by absorption of the modulated light, the heat generated in the sample is transferred to the gas in contact. Hence, the pressure in the air chamber oscillates at the chopping frequency which can be detected by the sensitive microphone. The photoacoustic signal being generated was then amplified by the preamplifier and further analyzed by using the lock-in amplifier. The photoacoustic signal amplitude is recorded as a function of the modulation frequency. All of our measurements were carried out at room temperature.

The electrical resistance of the superconducting ceramic samples was measured in the temperature range of 20 K–300 K by using four-point probe technique. However, the surface morphology and crystal plane of the samples were investigated by using scanning electron microscope, SEM (JEOL model 6400) and

TABLE I The samples thickness and thermal diffusivity values of  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Zn}_x\text{Cu}_3\text{O}_8$  ( $x = 0.02-0.10$ ),  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Ba}_x\text{Cu}_3\text{O}_8$  ( $x = 0.02-0.10$ ),  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{V}_x\text{Cu}_3\text{O}_8$  ( $x = 0.05-0.10$ ),  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Y}_x\text{Cu}_3\text{O}_8$  ( $x = 0.02-0.10$ ) and  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Sn}_x\text{Cu}_3\text{O}_8$  ( $x = 0.05-0.10$ )

Dopant M x	Zn		Ba		V		Y		Sn	
	$l_s$ (cm)	$\alpha$ ( $\text{cm}^2/\text{s}$ )	$l_s$ (cm)	$\alpha$ ( $\text{cm}^2/\text{s}$ )	$l_s$ (cm)	$\alpha$ ( $\text{cm}^2/\text{s}$ )	$l_s$ (cm)	$\alpha$ ( $\text{cm}^2/\text{s}$ )	$l_s$ (cm)	$\alpha$ ( $\text{cm}^2/\text{s}$ )
0.02	0.56	0.59	0.44	0.22	–	–	0.50	0.22	–	–
0.04	0.66	0.57	0.76	0.57	–	–	0.51	0.23	–	–
0.05	0.72	0.51	0.44	0.62	0.48	0.24	0.50	0.24	0.46	0.19
0.06	0.71	0.46	0.78	0.68	0.58	0.26	0.57	0.26	0.45	0.20
0.07	0.62	0.41	0.66	0.72	0.58	0.27	0.51	0.28	0.54	0.22
0.08	0.66	0.37	0.73	0.79	0.52	0.28	0.54	0.31	0.45	0.24
0.09	0.55	0.34	0.85	0.85	0.53	0.30	0.50	0.33	0.52	0.30
0.10	0.47	0.23	0.90	1.09	0.49	0.32	0.52	0.30	0.50	0.34

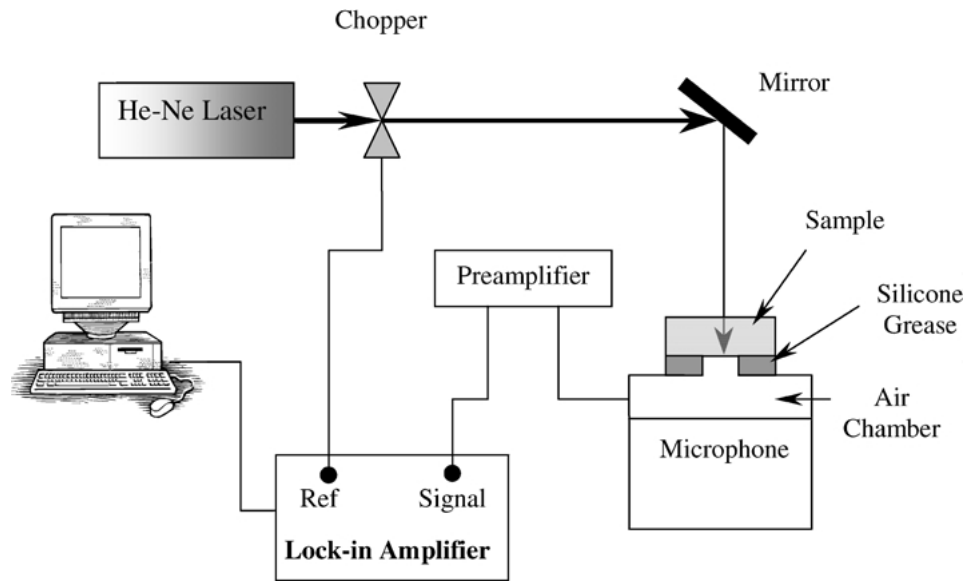


Figure 2 Experimental set-up for Open Photoacoustic Cell (OPC) technique.

X-Ray diffractometer, XRD (Siemens model D-5000) respectively.

### 3. Results and discussion

By using the analysis method proposed by Costa and Siqueira [13], we plot the  $\ln$  (PA signal) versus  $\ln(\sqrt{f})$  for 0.47 mm thick  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Zn}_x\text{Cu}_3\text{O}_\delta$  ( $x = 0.1$ ) sample as shown in Fig. 3. The characteristic

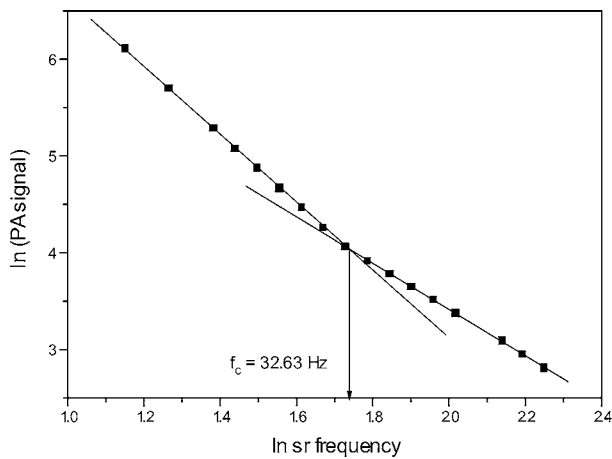


Figure 3 Plot  $\ln$  (PA signal) versus  $\ln(\sqrt{f})$  for 0.47 mm thick  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Zn}_x\text{Cu}_3\text{O}_\delta$  ( $x = 0.1$ ) sample.

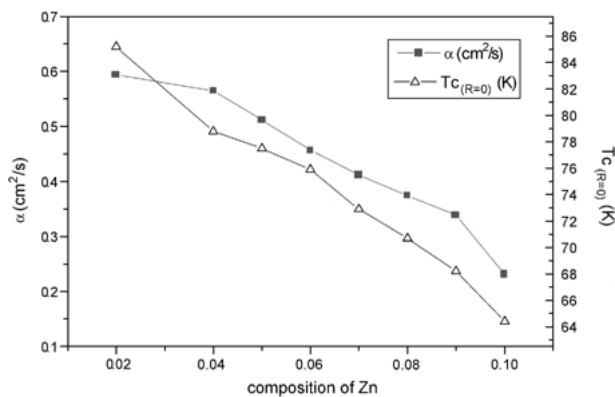


Figure 4 Thermal diffusivity and  $T_c$  values versus composition of Zn for  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Zn}_x\text{Cu}_3\text{O}_\delta$  ( $x = 0.02-0.10$ ) samples.

frequency,  $f_c$  (frequency at which the sample changes its behavior from thermally thick to thermally thin) was determined to be 32.63 Hz. The thermal diffusivity of this sample was then calculated as  $0.23 \text{ cm}^2/\text{s}$  by using Equation 3. The same procedure was used for the other superconductor composition and the measured thermal diffusivity values of all of our samples are listed in Table I.

The result for the thermal diffusivity as a function of the composition parameter  $x$  for  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Zn}_x$

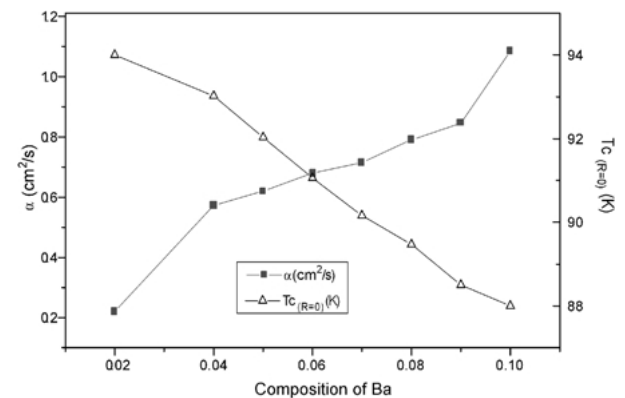


Figure 5 Thermal diffusivity and  $T_c$  values versus composition of Ba for  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Ba}_x\text{Cu}_3\text{O}_\delta$  ( $x = 0.02-0.10$ ) samples.

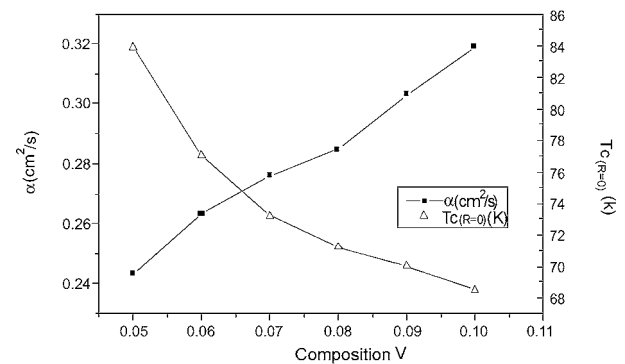


Figure 6 Thermal diffusivity and  $T_c$  values versus composition of V for  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{V}_x\text{Cu}_3\text{O}_\delta$  ( $x = 0.05-0.10$ ) samples.

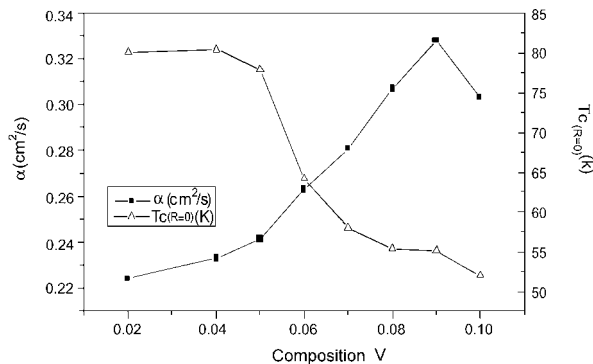


Figure 7 Thermal diffusivity and  $T_c$  values versus composition of Y for  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Y}_x\text{Cu}_3\text{O}_8$  ( $x = 0.02-0.10$ ) samples.

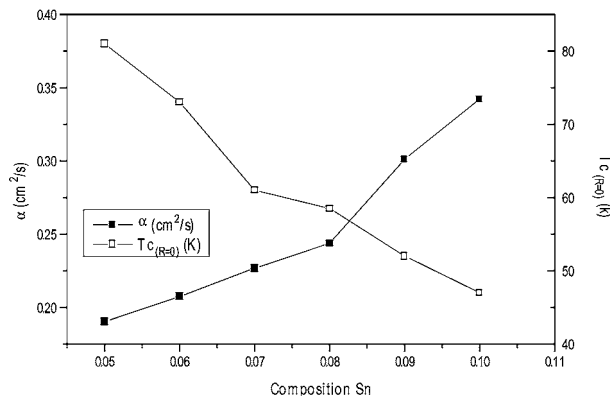


Figure 8 Thermal diffusivity and  $T_c$  values versus composition of Sn for  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Sn}_x\text{Cu}_3\text{O}_8$  ( $x = 0.05-0.10$ ) samples.

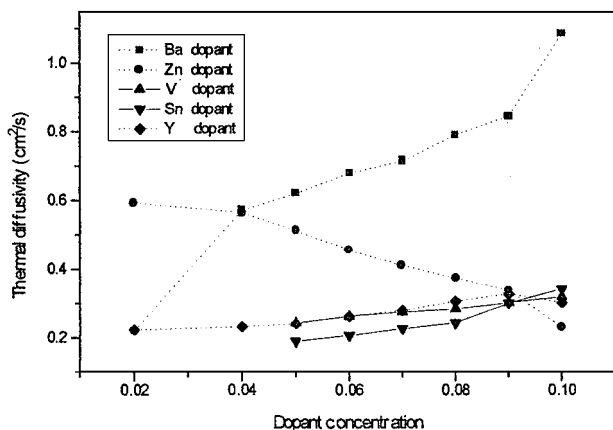
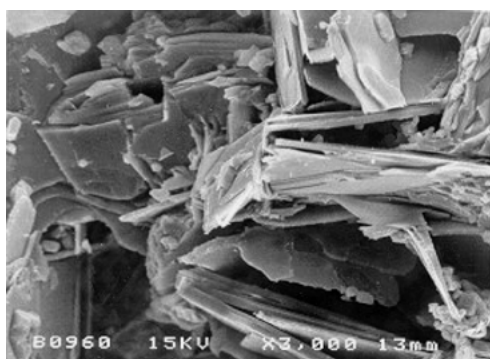
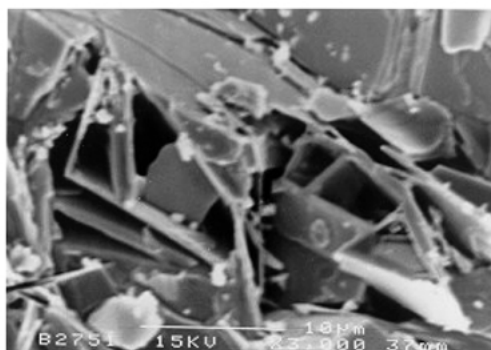


Figure 9 Thermal diffusivity as a function of dopant concentration for  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{M}_x\text{Cu}_3\text{O}_8$  ( $x = 0.05-0.10$ ,  $M = \text{Zn, Ba, V, Y}$  and  $\text{Sn}$ ) samples.



(a)



(b)

Figure 10 SEM micrographs of (a)  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Ba}_x\text{Cu}_3\text{O}_8$  ( $x = 0.06$ ) and (b)  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Zn}_x\text{Cu}_3\text{O}_8$  ( $x = 0.06$ ) samples.

$\text{Cu}_3\text{O}_8$  ( $x = 0.02-0.10$ ) sample is shown in Fig. 4. The thermal diffusivity values decrease with increasing mole fraction  $x$  of Zn, where the obtained values drop from  $0.59 \text{ cm}^2/\text{s}$  for  $x = 0.02$  to  $0.23 \text{ cm}^2/\text{s}$  for  $x = 0.10$ . Similarly, the value of  $T_{c(R=0)}$  decrease from  $85.2 \text{ K}$  ( $x = 0.02$ ) to  $64.4 \text{ K}$  ( $x = 0.10$ ) as more Zn dopant is added into the Ca side of the sample.

Figs 5 to 8 show the plot of the thermal diffusivity values versus dopant composition for  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Ba}_x\text{Cu}_3\text{O}_8$  ( $x = 0.02-0.10$ ),  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{V}_x\text{Cu}_3\text{O}_8$  ( $x = 0.05-0.10$ ),  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Y}_x\text{Cu}_3\text{O}_8$  ( $x = 0.02-0.10$ ) and  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Sn}_x\text{Cu}_3\text{O}_8$  ( $x = 0.05-0.10$ ) respectively. We note that, the measured thermal diffusivity values were in the range of  $(0.19-1.09) \text{ cm}^2/\text{s}$  where it increases when increasing the dopant (Ba, V, Y and Sn) concentration in the system. It is noted that in Fig. 7, for samples  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Y}_x\text{Cu}_3\text{O}_8$  ( $x = 0.02-0.10$ ), the thermal diffusivity value at  $x = 0.02$  is  $0.22 \text{ cm}^2/\text{s}$ . It increases with increasing dopant concentration until reaching a maximum at  $x = 0.09$  ( $\alpha = 0.33 \text{ cm}^2/\text{s}$ ). Above  $x = 0.09$ , the thermal diffusivity tends to decrease to  $0.30 \text{ cm}^2/\text{s}$  at  $x = 0.10$ .

On the other hand, the doping effect at the Ca sites of sample  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{M}_x\text{Cu}_3\text{O}_8$ , ( $M = \text{Ba, V, Y}$  and  $\text{Sn}$ ) does not favour the formation of high  $T_c$  phase. The behavior of  $T_{c(R=0)}$  in Figs 5-7 decrease with the increasing mole fraction  $x$  of the dopant.

Fig. 9 shows the summary of thermal diffusivity values as a function of dopant concentration for Zn, Ba, V, Y and Sn doped superconductor samples. In Fig. 10, we show the scanning electron microscope micrographs of  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Ba}_x\text{Cu}_3\text{O}_8$  ( $x = 0.06$ ) and  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Zn}_x\text{Cu}_3\text{O}_8$  ( $x = 0.06$ ) samples. The entire samples in this work exhibit a common feature of plate-like layer grains (2223 phase) randomly distributed homogeneous and less compact.

The XRD patterns for samples  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Ba}_x\text{Cu}_3\text{O}_8$  ( $x = 0.02-0.10$ ) and  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Zn}_x\text{Cu}_3\text{O}_8$  ( $x = 0.02-0.10$ ) are shown in Figs 11 and 12. Peaks belonging to 2223 phase are indicated by  $H(hkl)$  and for 2212 phase are indicated by  $L(hkl)$ . The volume fraction of the 2223 phase in the  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Ba}_x\text{Cu}_3\text{O}_8$  decrease from 84% to 70% as Ba doping increases from  $x = 0.02$  to  $x = 0.10$ . However, the volume fraction of the 2223 phase of the  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Zn}_x\text{Cu}_3\text{O}_8$  samples varies from 40% to 60%. Similar results were obtained for other samples.

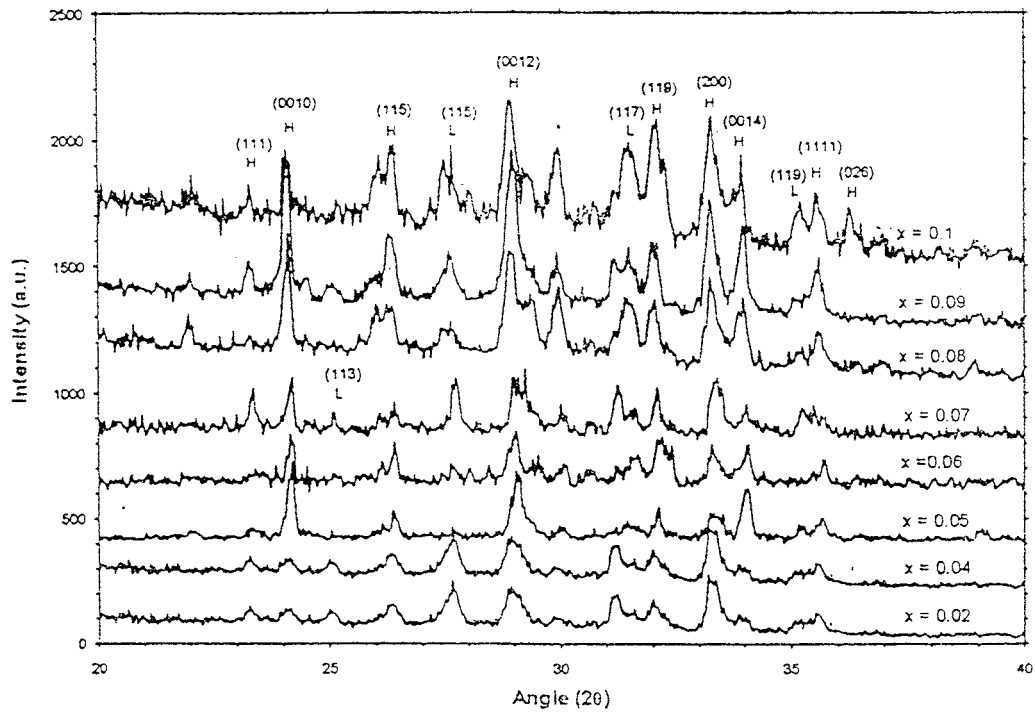


Figure 11 X-ray diffraction patterns of  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Ba}_x\text{Cu}_3\text{O}_8$  ( $x = 0.02-0.10$ ) samples.

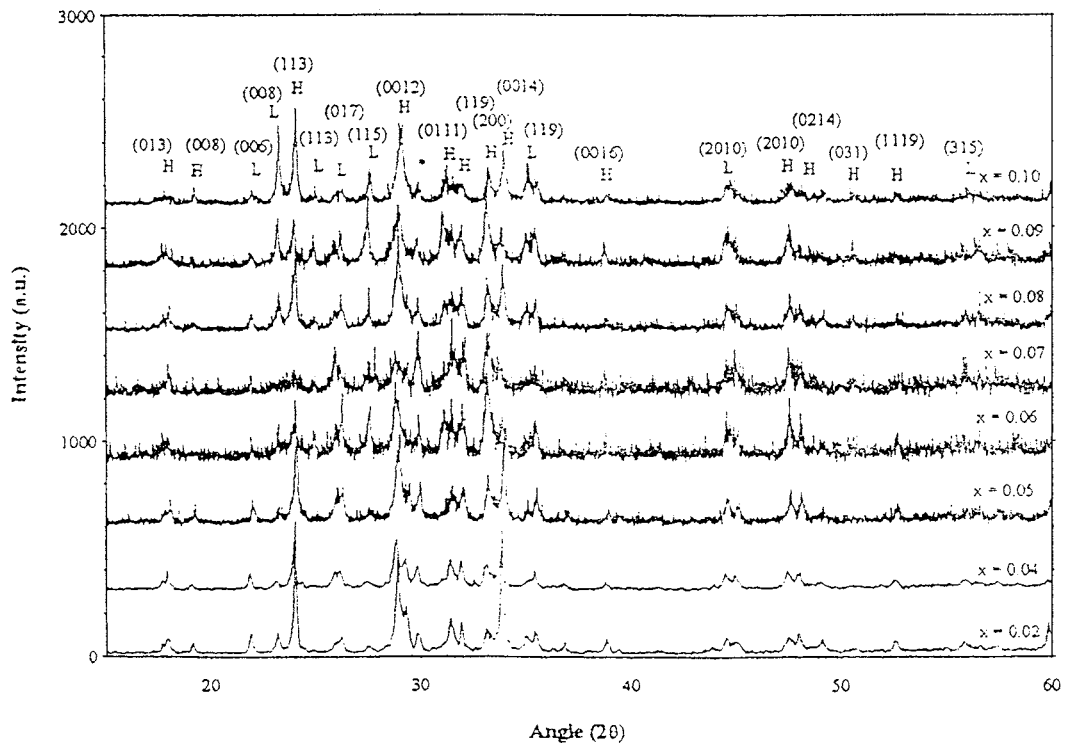


Figure 12 X-ray diffraction patterns of  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Zn}_x\text{Cu}_3\text{O}_8$  ( $x = 0.02-0.10$ ) samples.

#### 4. Conclusion

It has been shown that by using the simple open photoacoustic cell technique, the thermal diffusivity for  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{M}_x\text{Cu}_3\text{O}_8$ , (where  $M = \text{Zn}, \text{Ba}, \text{V}, \text{Y}$  and  $\text{Sn}$  and  $x = 0.02-0.10$ ) samples were obtained. The measured thermal diffusivity value was found to be very dependent on the dopant atom and dopant concentration. When Zn doping at the Ca sites in the  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{Zn}_x\text{Cu}_3\text{O}_8$  system, the measured thermal diffusivity decrease with the increasing of Zn content. However, the thermal diffusivity values in-

crease with the increasing of Ba, V, Y and Sn dopant in the  $\text{Bi}_2\text{Pb}_{0.6}\text{Sr}_2\text{Ca}_{2-x}\text{M}_x\text{Cu}_3\text{O}_8$  ( $M = \text{Ba}, \text{V}, \text{Y}$  and  $\text{Sn}$ ) system. It is seen that, for dopant concentration,  $x > 0.04$ , the Ba doped sample gives higher thermal diffusivity value than other dopant in the superconducting system.

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